One Twenty Phase Code Design with Good Discrimination Factor

S.P Singh¹, E.N.V. Purna Chandra Rao², S Babu Rao³ T D Bhatt⁴ ^{1&4} ECE Department, MGIT, Hyderabad, India ² ECE Department, CMR Institute of Technology, Hyderabad, India ³ ECE Department, MRCET, Hyderabad, India **singh spgahlot@rediffmail.com**

ABSTRACT

Sequences with good discrimination factor are useful for radar and communication applications. In this paper One Twenty Phase sequences are synthesized using Modified Genetic Algorithm (MGA). MGA is used as a statistical technique for obtaining approximate solutions to combinatorial optimization problems. This algorithm combines the good methodologies of the two algorithms like global minimum converging property of Genetic Algorithm (GA) and fast convergence rate of Hamming scan algorithm. The synthesized sequences have discrimination factor better than well known binary MPS code and Frank codes. The synthesized sequences also have complex signal structure which is difficult to detect and analyze by enemy electronics support measure.

Key words: Autocorrelation, Discrimination factor, Hamming scan, Polyphase codes, Genetic algorithm, Radar signal.

I INTRODUCTION

Sequences with low aperiodic autocorrelation sidelobe levels are useful for channel estimation, radar, and spread spectrum communication applications. Sequences achieving the minimum peak aperiodic autocorrelation sidelobe level one are called Barker Sequences.

The aperiodic autocorrelation function (ACF) of sequence S of length N is given by,

$$A(k) = \begin{cases} \sum_{n=0}^{N-k-1} s_n s_{n+k}^* ; & 0 \le k \le N-1 \\ \sum_{n=0}^{N+k-1} s_n s_{n-k}^* ; & -N+1 \le k \le 0 \end{cases} \qquad \dots \dots (1)$$

If all the sidelobes of the ACF of any polyphase sequence are bounded by

$$|A(k)| \le 1, \ 1 \le |k| \le N-1$$
 ... (2)

then the sequence is called a generalized Barker sequence or a polyphase Barker sequence. In 1953 [1] Barker introduced binary sequences for lengths N = 2,3,4,5,7,11, and 13, fulfilling the condition in eq. (2). The binary Barker can be regarded as a special case of polyphase Barker sequences. Binary codes that yield minimum peak sidelobes but do not meet the Barker condition are often called Minimum Peak Sidelobe (MPS) codes[2]. If the sequence elements are taken from an alphabet of size M, consisting of the Mth roots of unity.

$$S_{m} = \exp\left\{2\pi i \cdot \frac{m}{M}\right\} = \exp(i\phi_{m}) \qquad 0 \le m \le M - 1 \qquad (3)$$

the sequence is alternatively named an M-phase Barker sequence. In 1965, Golomb and Scholtz [3] first investigated generalized Barker sequences and presented six phases Barker sequence of lengths $N \le 13$. Recently, in [4] polyphase Barker sequences of lengths 46-63 were presented, wherein, an alphabet size of 2000 had to be used. However, polyphase Barker sequences for larger lengths require larger alphabets and the possibility for exhaustive search diminishes. The other well known polyphase codes with ideal autocorrelation are Frank codes [5]. Frank codes exist in perfect square length only. The synthesis of polyphase codes with good correlation properties is a nonlinear multivariable optimization problem, which is usually difficult to tackle. The Genetic Algorithm (GA) technique proved to be an efficient and powerful tool to find optimal or near optimal solutions for complex multivariable nonlinear functions but has slow convergence rate. The concept of Hamming scan algorithm has been employed for obtaining the pulse compression sequences at larger lengths with good correlation properties [6,7]. This algorithm has fast convergence rate but has demerit the viz., the tendency to be stuck with local minima. The MGA has global minimum estimation capability of GA algorithm and fast convergence rate of Hamming scan algorithm [6,7,8]. Binary code is one of the most commonly used radar pulse compression signals due to the easy signal generation and processing [2,9,10]. Polyphase signal has larger main lobe-to- peak sidelobe ratio over binary signal of the same code length. In addition, polyphase waveforms have a more complicated signal structure and thus, are more difficult to detect and analyze by an enemy's electronic support measures (ESMs). With the maturity of digital signal processing, the generation and processing of polyphase signals has become easy and less costly. Therefore, polyphase code is increasingly becoming a favorable alternative to the traditional binary code for radar signals and can be used as the basic code for radar signal design. In this paper, MGA has been used for the design of One Twenty Phase sequences with good correlation properties.

II. ONE TWENTY PHASE SEQUENCES

The One Twenty Phase sequence of length N bits is represented by a complex number sequence

$$\left\{ s(n) = e^{j\phi_m(n)}, n = 1, 2, ..., N \right\}$$
 (4)

Where $\phi_m(n)$ is the phase of nth bit in the sequence and lies between 0 and 2π . If the number of the distinct phases available to be chosen for each bit in a code sequence is M, the phase for the bit can only be selected from the following admissible values:

$$\begin{split} \phi_{\rm m}(n) &\in \left\{ 0, \, \frac{2\pi}{M}, \, 2\frac{2\pi}{M}, ..., \, (M-1)\frac{2\pi}{M} \right\} \quad ... \quad (5) \\ &= \left\{ \psi_1, \, \psi_2, ..., \psi_M \right\}. \end{split}$$

For example if M = 4, then values of $\{\psi_1, \psi_2, \psi_3 \text{ and } \psi_4\}$ will be 0, $\pi/2$, π and $3\pi/2$ respectively.

Considering a One Twenty Phase sequence S with code length N, one can concisely represent the phase values of S with the following 1 by N phase matrix:

$$S = [\phi_m(1), \phi_m(2), \phi_m(3), \dots, \phi_m(N)] \dots (6)$$

where all the elements in the matrix can only be chosen from the phase set in eq. (5).

A more practical approach to design One Twenty Phase sequences with properties in eq. (2) is to numerically search the best One Twenty phase sequences by minimizing a cost function that measures the degree to which a specific result meets the design requirements. For the design of One Twenty Phase sequences used in radar and communication the cost function is based on the sum of autocorrelation side lobe peaks. Hence, from eq. (1) the cost function can be written as,

$$E = \sum_{k=1}^{N-1} |A(k)| \qquad (7)$$

The minimization of cost function in eq. (7) generates a One Twenty Phase sequences that are automatically constrained by eq. (2). In this optimization we have minimize the autocorrelation sidelobe.

III. DISCRIMINATING FACTOR (DF)

The discriminating factor (DF) as defined by Golay is ratio of mainlobe peak value to the magnitude of sidelobe peak value of Autocorrelations function of sequence S. The DF, mathematically is defined as follows.

DF =
$$\frac{A(0)}{\max_{\substack{k \neq 0}} |A(k)|}$$
 ... (8)

The denominator is a measure of the peak sidelobe value and is related to the L_{∞} norm of the sidelobes.

IV. MODIFIED GENETIC ALGORITHM (MGA)

Modified Genetic Algorithm is proposed as a statistical technique for obtaining approximate solutions to combinatorial optimization problems. The proposed algorithm is a combination of Genetic Algorithm (GA) and Hamming Scan algorithms. It combines the good methodologies of the two algorithms like global minimum converging property of GA algorithm and fast convergence rate of Hamming scan algorithm. The demerit of Hamming scan algorithm is that it gets stuck in the local minimum point because it has no way to distinguish between local minimum point and a global minimum point. Hence it is sub-optimal. The drawback in Genetic algorithm is that it has a slow convergence rate because even though it may get closer to the global minimum point, it may skip it because of the methodology it employs. The MGA overcomes these drawbacks. It is quite effective to combine GA with Hamming Scan (HSA) Algorithm. GA tends to be quite good at finding generally good global solutions, but quite inefficient at finding the last few mutations to find the absolute optimum. Hamming Scan are quite efficient at finding absolute optimum in a limited region. Alternating MGA improve the efficiency of GA while overcoming the lack of robustness of HSA. MGA are introduced as a computational analogy of adaptive systems. They are modeled loosely on the principles of the evolution via natural selection, employing a population of individuals that undergo selection in the presence of variation-inducing operators such as mutation and recombination. A fitness function is used to evaluate individuals, and reproductive success varies with fitness.

V. RESULTS

One Twenty Phase sequences are designed using the MGA, the length of the sequence, N, is varied from 16 to 225. The cost function for the optimization is based on eq. (7). In this paper all, the DF values are obtained using Pentium - IV, processor. Table I shows the Comparison of Discrimination Factors of One Twenty Phase synthesized sequences with Binary MPS codes. In table I, column 1 shows sequence length, N, column 2 shows DF of binary MPS codes and column 3 shows the DF of One Twenty Phase sequences. Table II shows the Comparison of Discrimination Factors of One Twenty Phase synthesized sequences with Frank codes. In table II, column 1 shows sequence length, N, column 2 shows DF of Frank codes and column 3 shows the DF of One Twenty Phase sequences. The figs (1) and (2) are the graphical representation of DF comparison of Minimum Peak Sidelobe (MPS) Binary codes and Frank codes with synthesized One twenty-phase sequences whose values are shown in table I and II respectively. As shown in fig (1) and (2) the DF of One twenty-phase sequences are far better than both MPS binary and well known Frank codes. The synthesized sequence not only have better DF but also have a more complicated signal structure than Frank and binary codes, and thus, are more difficult to detect and analyze by an enemy's electronic support measures (ESMs). Fig(3) shows the comparison of Frank and One twenty phase sequence autocorrelation function of sequence length 225. As shown in the figure autocorrelation function of one twenty phase sequence is better than Frank code.

| Table –1 |
|---|
| Comparison of Discrimination Factor of One Twenty Phase synthesized |
| sequences with Binary MPS codes |

| Sequence | Binary MPS | One Twenty |
|----------|------------|------------|
| Length | codes | phase |
| | | sequences |
| 6 | 3.0 | 6 |
| 25 | 12.5 | 25 |
| 36 | 12.0 | 29.1 |
| 41 | 12.7 | 41 |
| 42 | 14.0 | 42 |
| 43 | 14.3 | 43 |
| 44 | 14.7 | 44 |

Table II Comparison of Discrimination Factor of One Twenty Phase synthesized sequences with Frank codes

| | r | r |
|----------|-------------|------------|
| Sequence | Frank codes | One Twenty |
| Length | | phase |
| _ | | Sequences |
| 16 | 11.3 | 16 |
| 25 | 15.5 | 25 |
| 36 | 18.0 | 29.1 |
| 49 | 21.8 | 27.8 |
| 64 | 24.4 | 40.9 |
| 81 | 28.1 | 37.2 |
| 100 | 30.9 | 41.4 |
| 121 | 34.4 | 44.6 |
| 225 | 47.0 | 63.7 |



Fig (1) Comparison of Discrimination Factor of Minimum peak Sidelobe Binary codes and One Twenty Phase sequences



Fig (2) Comparison of Discrimination Factor of Frank codes and One Twenty Phase sequences



Fig (3) Autocorrelation function of One twenty phase and Frank code of length 225

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Author Information

Dr. S P Singh received Master's and Ph.D degree from Osmania University. He worked for 18 years in the field of radar maintenance. Presently he is working as Professor and Head, Dept of ECE, Mahatma Gandhi Institute of Technology, Hyderabad, India. He has published 52 research papers in journals/ conferences. He is member of IEEE, Life member of ISTE (I), IE (I), and Fellow life member of IETE (I). His current interests are radar signal design and digital signal processing



Dr. T D Bhatt received Master's and Ph.D degree from Osmania and JNT University, Hyderabad respectively. He worked for 18 years in the field of radar maintenance. Presently he is working as Associate Professor in Dept of ECE Institute Mahatma Gandhi of Technology, Hyderabad. He has published 18 research papers in journals/ conferences. He is Life member of ISTE (I) and Fellow life member of IETE. His current interests are radar signal design and digital signal processing



Mr E. N. V. Purna Chandra Rao was born in Eluru (A.P), India. He received Master's degree from JNTUA, Ananantapur and Pursuing Ph.D. He worked for 15 years in the field of Radar and Missiles System. Presently, he is working as Associate Professor in CMR Institute of Technology, Hyderabad, India.